

LP ①

**SET-UP** the following LP problems. Do not solve.

Example 1: Secretaries vs. Clerks: (a min  $C$  problem)

The Handy Company has determined that a secretary can type 8 pages and file 20 reports per hour, and a clerk can type 4 pages and file 40 reports per hour. After extensive research the company has determined that each hour it needs 320 pages typed and 2600 reports filed. If secretaries are paid \$11 per hour and clerks are paid \$5 per hour, how many secretaries and clerks should the Handy Company hire to meet its needs at a minimum cost?

**Set-up:**

|                                 |                                    |
|---------------------------------|------------------------------------|
| (objective fn.)                 | $\min C = 11x_1 + 5x_2$            |
| ( pages typed/hr. constraint)   | $8x_1 + 4x_2 \geq 320$             |
| ( reports filed/hr. constraint) | $20x_1 + 40x_2 \geq 2600$          |
| ( non-negativity constraint)    | $x_1, x_2 \geq 0$                  |
| (variable dictionary)           | $x_1 = \#$ secretaries to be hired |
|                                 | $x_2 = \#$ clerks to be hired      |

Example 2: Fred's Hats: (a max  $P$  problem)

Fred's Hats produces two types of cowboy hats. Each type 1 hat takes Fred 15 minutes to make while each type 2 hat takes him only 10 minutes. Each type 1 hat uses  $1/2$  square yard of material and each type 2 hat uses  $3/4$  square yard of material. Each work day consists of 7 hours. There are 125 square yards of material on hand each work day. If the profit on each type 1 hat is \$9 and the profit on each type 2 hat is \$7, how many hats of each type should Fred make each day in order to maximize his daily profit?

**Set-up:**

$$\begin{aligned} \max P &= 9x_1 + 7x_2 \\ 15x_1 + 10x_2 &\leq 420 \\ \frac{x_1}{2} + \frac{3x_2}{4} &\leq 125 \\ x_1, x_2 &\geq 0 \end{aligned}$$

$$\begin{aligned} x_1 &= \# \text{ of type 1 hats to be made each day} \\ x_2 &= \# \text{ of type 2 hats to be made each day} \end{aligned}$$