

# Ontario

Math 282 Spring 2011 Exam 1

Name \_\_\_\_\_

15 problems, 10 points each As always SHOW WORK.

Use the following information for problems 1) and 2). The time in seconds for five rats to complete a maze were 24, 37, 38, 43, and 33.

1) Find the sample mean and median of these numbers.

24 33 37 38 43  
↑  
m

$$\frac{\sum x}{n} = \frac{175}{5} = (\bar{x} = 35, m = 37)$$

2) Find the standard deviation s of these numbers.

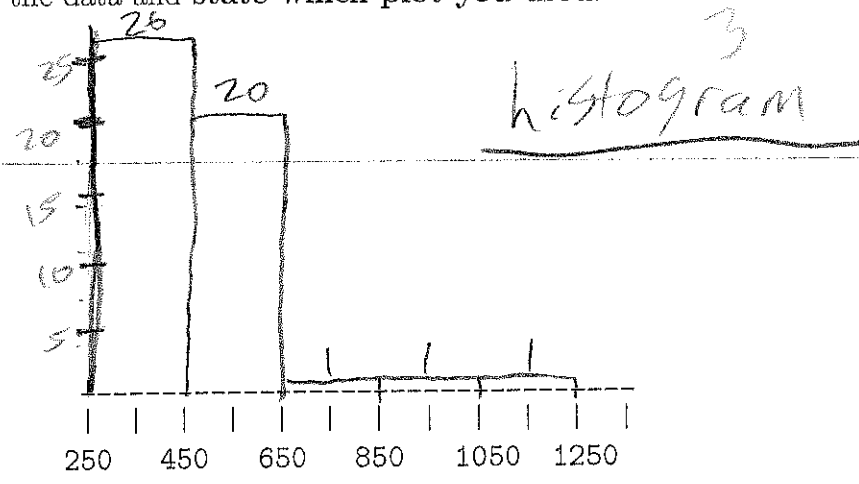
x	x - $\bar{x}$	(x - $\bar{x}$ ) <sup>2</sup>
24	-11	121
33	-2	4
37	2	4
38	3	9
43	8	64

$$202 = \sum (x - \bar{x})^2$$

$$s = \sqrt{\frac{\sum (x - \bar{x})^2}{n-1}} = \sqrt{\frac{202}{4}} = \sqrt{50.5} = 7.1063$$

3) Data for federal aid per capita for the 50 states in 1986 is summarized below. Make a histogram or bar graph of the data and state which plot you used.

class	count
250 ≤ < 450	26
450 ≤ < 650	20
650 ≤ < 850	1
850 ≤ < 1050	1
1050 ≤ < 1250	1



Use the following information for problems 4), 5) and 6). Suppose that white tailed deer are caught, tagged and fitted with a small radio transmitter. Several months later, the deer are tracked and the distance  $X$  from the release point is recorded. The distances were approximately normal with a mean of 3200 feet and a standard deviation of 960 feet.

4) What distance  $X$  must a randomly selected deer travel from the release point in order for the distance to be in the top 10%?

~~$X \sim N(\mu, \sigma)$~~  
$$\begin{array}{r|l} 03 & 09 \text{ tail} \\ 1.2 & .9997 \quad .9015 \end{array} \quad z^* = 1.28$$

$$X^* = \mu + \sigma z^* = 3200 + 960(1.28) = \boxed{4428.8}$$

$1.28 \quad 4428.8 \quad -3 \quad -1.28 \quad -5$

5) Find the probability that  $X$  will be greater than 4000.



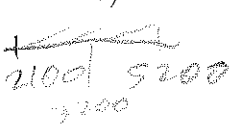
$$\frac{4000 - 3200}{960} = 0.83$$

$$\begin{array}{r|l} 03 & \\ 0.8 & .7967 \end{array}$$



$$P(X > 4000) = 1 - .7967 = \boxed{0.2033}$$

6) Find the probability that  $X$  will be between 2100 and 5200.



$$z = \frac{2100 - 3200}{960} = -1.15$$

$$z = \frac{5200 - 3200}{960} = 2.08$$

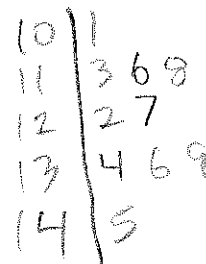
$$\begin{array}{r|l} 05 & 08 \\ -1.1 & .1251 \\ 2.0 & .9812 \end{array}$$

$$\text{Prob} = .9812 - .1251 = \boxed{0.8561}$$

e 7) Suppose that the scores on 10 makeup history finals are listed below.

- 122 101 145 113 116 127 139 118 134 136

Make a stem plot for the data. Do not forget to include the stem and leaf units.



stem tens  
leaf ones

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Use the following information for 8) and 9). The table below will be used to find the correlation  $r$  between  $x$  and  $y$ . Note that  $\bar{x} = 58.2$ ,  $s_x = 13.198$ ,  $\bar{y} = 66.0$ , and  $s_y = 15.890$ .

x	y	$z_x = (x - \bar{x})/s_x$	$z_y = (y - \bar{y})/s_y$	$z_x z_y$
38	41	-1.5305	-1.5733	2.4080
56	63	-0.1667	-0.1888	0.0315
59	70	.0606	0.2517	.01525
64	72	0.4395	0.3776	0.1659
74	84	1.1972	1.1328	1.3561

8) Fill in the table, show work.

$$z_x = \frac{59 - 58.2}{13.198} = .0606, z_y = \frac{70 - 66}{15.89} = 0.2517$$

$$z_x z_y = (.0606)(.2517) = .01525$$

9) After completing 8), use the above table to find the correlation  $r$  between  $x$  and  $y$ .

$$r = \frac{\sum z_x z_y}{n-1} = \frac{3.97675}{4} = \boxed{.9942} = \frac{3.9768}{4}$$

Use the following information for problems 10) and 11). It is desired to predict *calories* (consumed per day) from a person's *weight* (in kilograms). The least squares equation is  $\hat{y} = 112.16 + 26.90x$ .

10) What is the response variable?

calories

or -9

11) Predict the calories if weight = 50.

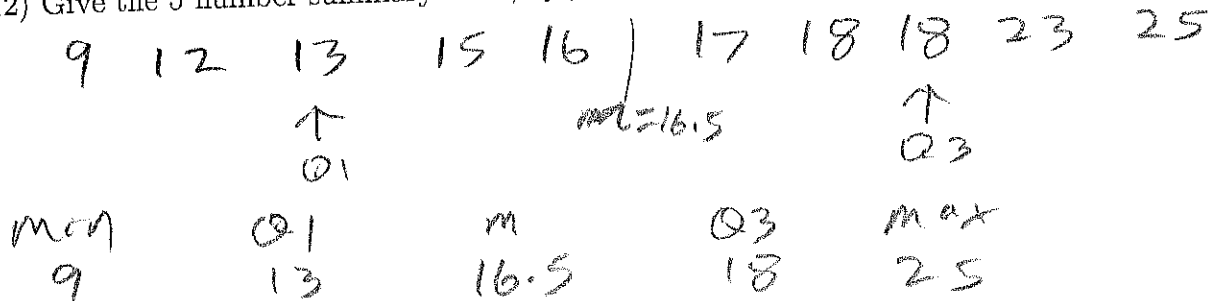
$$\hat{y} = 112.16 + 26.9(50) = \boxed{1457.16}$$

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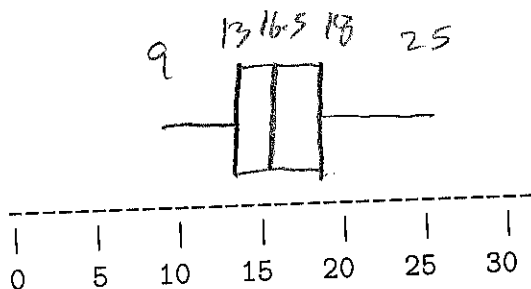
9 16 23 25 17 12 13 15 18 18

Use the following information for problems 12) and 13). The numbers above are number of people bitten by alligators in Florida for years 1998 to 2007.

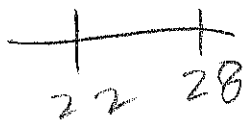
12) Give the 5 number summary: min, Q1, median, Q3, and max. SHOW WORK.



13) Draw a box plot for the alligator bite data.



14) Suppose the ACT score  $X$  is approximately normal with mean  $\mu = 22$  and standard deviation  $\sigma = 3$  points. Find the probability that a randomly selected ~~midterm~~ ACT score is less than 28.



$$z = \frac{28 - 22}{3} = 2.00$$

$$\frac{100}{20} = 5.0$$

$$P(X < 28) = 0.9772$$

$1 - 0.9772 = 0.0228$

15) Suppose that  $\sum(x_i - \bar{x})^2 = 6016$  and  $n = 60$ . Find the standard deviation  $s$ .

$$s = \sqrt{\frac{\sum(x_i - \bar{x})^2}{n-1}} = \sqrt{\frac{6016}{59}} = \sqrt{101.996} = 10.0978$$