

01008

1) Suppose that for fully continuous whole life insurance on (x) you are given that the force of mortality is constant. Then $\bar{A}_x = \bar{A}_{x+t}$ and $\bar{a}_x = \bar{a}_{x+t}$ do not depend on $t \geq 0$. Hence $\text{Var}({}_tL) = \text{Var}({}_0L) = \text{Var}({}_t\bar{L}(\bar{A}_x)) = {}^2\bar{A}_x$. Find $\text{Var}({}_t\bar{L}(\bar{A}_x)) = \text{Var}({}_tL)$ if $\mu = 0.01$ and $\delta = 0.04$.

$$= \frac{\mu}{\mu + \delta} = \frac{.01}{.01 + .04} = \boxed{\frac{1}{9} = 0.1111}$$

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2) For discrete whole life insurance on (45) , mortality follows the illustrative life table and $i = 0.06$. Calculate ${}_{15}V_{45}$ using

a) the annuity ratio formula

$$1 - \frac{\ddot{a}_{60}}{\ddot{a}_{45}} = 1 - \frac{11.1454}{14.1121} = \boxed{0.2102}$$

b) the insurance ratio formula. $= \frac{A_{x+t} - A_x}{1 - A_x}$ table gives $1000A_x$
 $= \frac{A_{60} - A_{45}}{1 - A_{45}}$

$$= \frac{.36913 - .2012}{1 - .2012} = \boxed{0.2102}$$

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3) Suppose $\bar{a}_x = 16.77$, and $\bar{a}_{x+20} = 12.62$. Find the terminal reserve ${}_{20}\bar{V}(\bar{A}_x)$.

$$1 - \frac{\bar{a}_{x+20}}{\bar{a}_x} = 1 - \frac{12.62}{16.77} = \boxed{0.2475}$$

4) Calculate \bar{a}_{x+t} given ${}_tV(\bar{A}_x) = 0.1$, $\bar{P}(\bar{A}_x) = 0.0105$ and $\delta = 0.03$.

Hint: $\bar{A}_{x+t} = 1 - \delta \bar{a}_{x+t}$. Use the formula for ${}_tV(\bar{A}_x)$ and solve for \bar{a}_{x+t} .

$$\begin{aligned} 1 &= {}_tV(\bar{A}_x) = \bar{A}_{x+t} - \bar{P}(\bar{A}_x) \bar{a}_{x+t} = 1 - \delta \bar{a}_{x+t} - \bar{P}(\bar{A}_x) \bar{a}_{x+t} \\ &= 1 - \bar{a}_{x+t} [0.03 + 0.0105] \quad \text{so} \end{aligned}$$

$$\bar{a}_{x+t} = \frac{1 - 0.1}{0.03 + 0.0105} = \frac{0.9}{0.0405} = \boxed{22.2222}$$

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5) For h -pay insurance, if $t \geq h$ then there are no benefits premiums left to pay, so ${}_tV = (\text{APV insurance}) - (\text{APV future benefits}) = \text{APV insurance at time } t$. Consider a fully discrete 20-pay whole life insurance of 1000 on (50) where mortality follows the illustrative life table, $i = 0.06$. Calculate ${}_{20}V$ ($= {}_{20}^{20}V$), the 20th terminal benefit reserve.

$${}_tV = A_{x+t} \quad \text{for } t \geq h$$

$$\text{so } {}_{20}^{20}V = 1000 A_{50+20} = 1000 A_{70}$$

$$= \boxed{514.95}$$

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