1. Find the general solution $y_{h}$ for each of the following.
a) $y^{\prime \prime}+3 y^{\prime}-18 y=0$
b) $9 y^{\prime \prime}+6 y^{\prime}+y=0$
c) $y^{\prime \prime}-4 y^{\prime}+5 y=0$
d) $y^{\prime \prime}+y^{\prime}-y=0$
2. Consider the problem (see more homework problems)

$$
x^{2} y^{\prime \prime}-x(x+2) y^{\prime}+(x+2) y=0
$$

a) Show that $y=x$ is one solution.
b) Find the second solution.
3. Solve the IVP using two methods. (see more for sect. 3.4 and 3.5 )

$$
\begin{aligned}
y^{\prime \prime}+4 y^{\prime} & =36 t^{2}+34 t \\
y(0) & =0 \\
y^{\prime}(0) & =0
\end{aligned}
$$

4. Consider the problem

$$
y^{\prime \prime}-c y^{\prime}+y=0
$$

for some constant $c$. Describe how the behavior of this solution changes as $c$ varies.

